

1. Convert 1 day to s.

$$1 \text{ day} \times \frac{24 \text{ hrs}}{1 \text{ day}} \times \frac{60 \text{ min}}{1 \text{ hr}} \times \frac{60 \text{ s}}{1 \text{ min}} = 86,400\text{s}$$
$$= 8.64 \times 10^4 \text{ s}$$

Answer: 1 day =  $8.64 \times 10^4$  s

2. The orbital period of Neptune is 164.793 yrs. Convert it to min.

$$164.793 \text{ yrs} \times \frac{365.25 \text{ days}}{1 \text{ yr}} \times \frac{24 \text{ hrs}}{1 \text{ day}} \times \frac{60 \text{ min}}{1 \text{ hr}} = 86,674,526.28 \text{ min}$$
$$= 8.667452628 \times 10^7 \text{ min}$$

Answer: 164.793 yrs =  $8.667452628 \times 10^7$  min

3. The equatorial radius of Jupiter is 71,494 km. Convert it to cm.

$$71,494 \text{ km} \times \frac{1,000 \text{ m}}{1 \text{ km}} \times \frac{100 \text{ cm}}{1 \text{ m}} = 7,149,400,000 \text{ cm}$$
$$= 7.1494 \times 10^9 \text{ cm}$$

Answer: 71,494 km =  $7.1494 \times 10^9$  cm

4. Convert the orbital velocity of Mercury, 47.89 km/s, to m/hr.

$$\frac{47.89 \text{ km}}{1 \text{ s}} \times \frac{1,000 \text{ m}}{1 \text{ km}} \times \frac{60 \text{ s}}{1 \text{ min}} \times \frac{60 \text{ min}}{1 \text{ hr}} = 172,404,000 \text{ m/hr}$$
$$= 1.72404 \times 10^8 \text{ m/hr}$$

Answer: 47.89 km/s =  $1.72404 \times 10^8$  m/hr

5. Convert the average density of Saturn,  $0.69 \text{ g/cm}^3$ , to  $\text{kg/m}^3$ .

$$\frac{0.69 \text{ gm}}{1 \text{ cm}^3} \times \frac{1 \text{ kg}}{1,000 \text{ g}} \times \left( \frac{100 \text{ cm}}{1 \text{ m}} \right)^3$$

$$= 690 \text{ kg/m}^3 = 6.90 \times 10^2 \text{ kg/m}^3$$

Answer:  $0.69 \text{ gm/cm}^3 = 6.90 \times 10^2 \text{ kg/m}^3$

6. Convert the distance in ly, 4.24, to the closest star, Proxima Centauri to km.

$$4.24 \text{ ly} \times \frac{9.46 \times 10^{12} \text{ km}}{1 \text{ ly}} = 4.01104 \times 10^{13} \text{ km}$$

Answer:  $4.24 \text{ ly} = 4.01104 \times 10^{13} \text{ km}$

7. The speed of the space shuttle is about 17,600 miles/hr. How many years would it take the space shuttle to reach Proxima Centauri?

$$\frac{17,600 \text{ miles}}{1 \text{ hr}} \times \frac{1.6 \text{ km}}{1 \text{ mile}} = \frac{28,160 \text{ km}}{1 \text{ hr}}$$

$$4.01104 \times 10^{13} \text{ km} \times \frac{1 \text{ hr}}{28,160 \text{ km}} = 1.424375 \times 10^9 \text{ hr}$$

$$1.424375 \times 10^9 \text{ hr} \times \frac{1 \text{ day}}{24 \text{ hrs}} \times \frac{1 \text{ yr}}{365.25 \text{ days}} = 162488 \text{ yrs} = 1.62488 \times 10^5 \text{ yrs}$$

Answer: It would take the space shuttle  $1.62488 \times 10^5$  yrs to reach Proxima Centauri.

8. How long does light from the Sun take to reach the Earth in min?

distance = rate x time

$$\text{time} = \frac{\text{distance}}{\text{rate}}$$

$$\text{rate} = c = 3 \times 10^5 \text{ km/s}$$

$$\text{distance} = d_{\text{Sun-Earth}} = 1.496 \times 10^8 \text{ km}$$

$$\text{time} = \frac{d_{\text{Sun-Earth}}}{c} = 1.496 \times 10^8 \text{ km} \times \frac{1 \text{ s}}{3 \times 10^5 \text{ km}}$$

$$498.667 \text{ s} \times \frac{1 \text{ min}}{60 \text{ s}} = 8.31 \text{ min}$$

Answer: Light from the Sun takes  $8.316 \times 10^1$  min to reach Earth.

9. Convert the mass of Pluto,  $0.0022 M_{\text{Earth}}$ , to kg:

$$M_{\text{Earth}} = 5.976 \times 10^{24} \text{ kg}$$

$$0.0022 M_{\text{Earth}} = 0.0022 \times 5.976 \times 10^{24} \text{ kg} = 1.31472 \times 10^{22} \text{ kg}$$

Answer:  $0.0022 M_{\text{Earth}} = 1.31472 \times 10^{22} \text{ kg}$

10. Sirius has a radius of  $2.1 R_{\text{Sun}}$ . Convert it to m.

$$R_{\text{Sun}} = 695,000 \text{ km}$$

$$2.1 R_{\text{Sun}} = 2.1 \times 695,000 \text{ km} = 1,459,500 \text{ km}$$

$$1,459,500 \text{ km} \times \frac{1,000 \text{ m}}{1 \text{ km}} = 1,459,500,000 \text{ m} = 1.4595 \times 10^9 \text{ m}$$

Answer:  $2.1 R_{\text{Sun}} = 1.4595 \times 10^9 \text{ m}$

11. The star Betelgeuse is 420 ly away. This means that the light we see from that star left it 420 years ago. Convert 420 yrs to Cosmic Calendar time in s.

$$\text{Cosmic Calendar time} = \frac{\text{real time}}{1.2 \times 10^{10}} = \frac{420 \text{ yrs}}{1.2 \times 10^{10}} = 3.5 \times 10^{-8} \text{ yrs}$$

$$= 3.5 \times 10^{-8} \text{ yrs} \times \frac{365.25 \text{ days}}{1 \text{ yr}} \times \frac{24 \text{ hrs}}{1 \text{ day}} \times \frac{60 \text{ min}}{1 \text{ hr}} \times \frac{60 \text{ s}}{1 \text{ min}} = 1.104516 \text{ s}$$

Answer:  $420 \text{ yrs} = 1.104516 \text{ s}$  on the Cosmic Calendar

12. Convert the tilt of the Earth's axis of rotation,  $23.5^\circ$ , from the ecliptic plane to degrees and arcminutes.

Subtract the integer part:  $23.5 \text{ d} - 23 \text{ d} = 0.5 \text{ d}$

$$0.5 \text{ d} \times \frac{60'}{1 \text{ d}} = 30'$$

$$23 \text{ d} + 0.5 \text{ d} = 23.5 \text{ d}$$

Answer:  $23.5 \text{ d} = 23 \text{ d } 30'$

13. The declination,  $d$ , of the star Procyon is  $05 \text{ d } 13' 30''$ . Convert it to arcseconds.

$$\begin{aligned} \left( 5 \text{ d} \times \frac{3,600''}{1 \text{ d}} \right) + \left( 13' \times \frac{60''}{1'} \right) + 30'' \\ = 18,000'' + 780'' + 30'' = 18,810'' \end{aligned}$$

Answer:  $05 \text{ d } 13' 30'' = 18,810''$

14. Convert the right ascension of the star Pollux,  $07 \text{ h } 45 \text{ m } 14.5 \text{ s}$ , to h.

$$\begin{aligned} 7 \text{ h} + \left( 45 \text{ m} \times \frac{1 \text{ h}}{60 \text{ m}} \right) + \left( 14.5 \text{ s} \times \frac{1 \text{ h}}{3,600 \text{ s}} \right) \\ = 7 \text{ h} + 0.75 \text{ h} + 0.00403 \text{ h} = 7.75403 \text{ h} \end{aligned}$$

Answer:  $07 \text{ h } 45 \text{ m } 14.5 \text{ s} = 7.75403 \text{ h}$

15. The angular distance between Antares and Shaula,  $17 \text{ d } 16' 49''$ . Convert it to degrees.

$$\begin{aligned} 17 \text{ d} + \left( 16' \times \frac{1 \text{ d}}{60'} \right) + \left( 49'' \times \frac{1 \text{ d}}{3,600''} \right) \\ = 17 \text{ d} + 0.267 \text{ d} + 0.0136 \text{ d} = 17.2806 \text{ d} \end{aligned}$$

Answer:  $17 \text{ d } 16' 49'' = 17.2806 \text{ d}$

16. The angular distance between the stars Caph and Schedar is  $4.91472^\circ$ . Convert it to degrees, arcminutes, and arcseconds.

$$\text{Subtract the integer part: } 4.91472d - 4d = 0.91472d$$

$$0.91472d \times \frac{60'}{1d} = 54.8832'$$

$$\text{Subtract the integer part: } 54.8832' - 54' = 0.8832'$$

$$0.8832' \times \frac{60''}{1'} = 53''$$

$$\text{Answer: } 4.91472^\circ = 4d 54' 53''$$

17. The synodic period of the Moon is 29 days 12h 44m 2.82s. Convert it to days.

$$12 \text{ hr} \times \frac{1 \text{ day}}{24 \text{ hr}} = 0.5 \text{ days}$$

$$44 \text{ min} \times \frac{1 \text{ hr}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ hr}} = 0.0306 \text{ days}$$

$$2.82 \text{ s} \times \frac{1 \text{ min}}{60 \text{ s}} \times \frac{1 \text{ hr}}{60 \text{ min}} \times \frac{1 \text{ day}}{24 \text{ hr}} = 0.000033 \text{ days}$$

$$29 \text{ days} + 0.5 \text{ days} + 0.0306 \text{ days} + 0.0000326 \text{ days} = 29.531 \text{ days}$$

$$\text{Answer: } 29 \text{ days } 12\text{h } 44\text{m } 2.82\text{s} = 29.531 \text{ days}$$

18. The surface temperature of Venus is  $882^\circ\text{F}$ . Convert it to both  $^\circ\text{C}$  and K.

$$^\circ\text{C} = \frac{5}{9} (882^\circ\text{F} - 32^\circ\text{F}) = 472.2^\circ\text{C}$$

$$\text{K} = 472.2^\circ\text{C} + 273^\circ\text{C} = 745.2\text{K}$$

$$\text{Answer: } 882^\circ\text{F} = 472.2^\circ\text{C} = 745.2\text{K}$$

19. The temperature of the star Sirius is 9,150 K. Convert it to both °C and °F.

$$^{\circ}\text{C} = \text{K} - 273^{\circ}\text{C} = 9,150 \text{ K} - 273^{\circ}\text{C} = 8,877^{\circ}\text{C}$$

$$^{\circ}\text{F} = \frac{9}{5} (^{\circ}\text{C}) + 32^{\circ}\text{F} = \frac{9}{5} (8,877^{\circ}\text{C}) + 32^{\circ}\text{F} = 16,010.6^{\circ}\text{F}$$

$$\text{Answer: } 9,150 \text{ K} = 8,877^{\circ}\text{C} = 16,010.6^{\circ}\text{F}$$

20. Pluto is 39.44 AU from the Sun. Calculate the approximate area of the solar system in  $\text{km}^2$ . Assume that Pluto marks the edge of our solar system and its distance from the Sun is the radius of our solar system. Remember that the formula for area is  $A = \pi r^2$ .

$$A_{\text{solar system}} = 3.14 \times (39.44 \text{ AU})^2 = 3.14 \times 1,555.51 \text{ AU}^2 = 4,884.313 \text{ AU}^2$$

$$= 4,884.313 \text{ AU}^2 \times \left( \frac{1.496 \times 10^8 \text{ km}}{1 \text{ AU}} \right)^2 = 1.0931 \times 10^{20} \text{ km}^2$$

$$\text{Answer: The area of the solar system is } 1.0931 \times 10^{20} \text{ km}^2$$

21. The radius of the Sun is 695,000 km. The radius of the Earth is 6,378 km. Calculate how many Earths would fit inside the Sun. Remember that the formula for volume is

$$V = \frac{4}{3} \pi r^3 .$$

$$V_{\text{Sun}} = \frac{4}{3} \pi \times (695,000 \text{ km})^3$$

$$V_{\text{Earth}} = \frac{4}{3} \pi \times (6,378 \text{ km})^3$$

$$\begin{aligned} \frac{V_{\text{Sun}}}{V_{\text{Earth}}} &= \frac{\frac{4}{3} \pi \times (695,000 \text{ km})^3}{\frac{4}{3} \pi \times (6,378 \text{ km})^3} = \frac{(695,000 \text{ km})^3}{(6,378 \text{ km})^3} \\ &= \frac{3.36 \times 10^{17} \text{ km}^3}{2.59 \times 10^{11} \text{ km}^3} = 1,293,900 \text{ Earths} = 1.2939 \times 10^6 \text{ Earths} \end{aligned}$$

$$\text{Answer: } 1.2939 \times 10^6 \text{ Earths would fit inside the Sun.}$$

22. The amount of mass contained in stars in our neighborhood is about  $0.039 M_{\text{Sun}}/\text{parsec}^3$  (Sky & Telescope, p. 44, June, 1999). Convert it to  $\text{kg}/\text{m}^3$ .

$$M_{\text{Sun}} = 1.989 \times 10^{30} \text{ kg}$$

$$0.039 M_{\text{Sun}} = 0.039 \times 1.989 \times 10^{30} \text{ kg} = 7.7571 \times 10^{28} \text{ kg}$$

$$1 \text{ parsec}^3 = 1 \text{ parsec} \times \text{parsec} \times \text{parsec}$$

$$1 \text{ parsec}^3 \times \left( \frac{3.26 \text{ ly}}{1 \text{ parsec}} \right)^3 = 34.646 \text{ ly}^3$$

$$34.646 \text{ ly}^3 = 34.646 \text{ ly} \times \text{ly} \times \text{ly}$$

$$34.646 \text{ ly}^3 \times \left( \frac{9.46 \times 10^{15} \text{ m}}{1 \text{ ly}} \right)^3 = 2.933 \times 10^{49} \text{ m}^3$$

$$0.039 M_{\text{Sun}}/\text{parsec}^3 = \frac{7.7571 \times 10^{28} \text{ kg}}{2.933 \times 10^{49} \text{ m}^3} = 2.6448 \times 10^{-21} \text{ kg}/\text{m}^3$$

$$\text{Answer: } 0.039 M_{\text{Sun}}/\text{parsec}^3 = 2.6448 \times 10^{-21} \text{ kg}/\text{m}^3$$